## multinte Regression

Simple Represen:-- Study of 2 vointles (one is Independent other is dependent - 11002 C. John Commenter Veed for prediction of change of dependent v virles of according to charge of Independent v milles). Regression (Y) = R + bx /nlepredet her cutent PAP Independent vairble Dependent virble 8 to Am Viable Carre effet verde Cole-1 price 50 Salle 5, NW Cape-2 pri ce 60 Sales y,now Coll-3 price 40 5 aleq 6, mw Coll - 4 price 5'5 Solle Call - 5 pria Erleg 35

Fm

Maltirt Reportem - Many varmelles (Mrethen 2) Dependent Vintle Trependent Intérentes predict of change of chance in Indepentiverable. Pree(Iva). AArt(iva) ! Stales, 21 Cor-1 comos 2 m 00 220 m Gow w Coen - 2 40 down 15000 Con - 3 60 2 3 0 m 11 4 55 11 5 5 mm Jur on 45 6 120ma moetiMe Robresson # melhide of 1 Least squee Methor (direct) Plant some method ming means
((x) / shot cont method)

(2)

Least Sque value aling mean (3+1) on (2+1) mello) (when (2+1) men) (3+1) on (2+1) weher  $\alpha_1 = (\chi_1 - \bar{\chi}_1)$ ,  $\chi_2 = (\chi_2 - \bar{\chi}_2)$  $x_{2} = (x_{3} - \overline{x_{3}})$ 8 2, = b<sub>12.3</sub> 2 + b<sub>13.2</sub> 2<sub>3</sub> nehere 6,2.3 & 5/3.2 = partial regular Co. Miccor Holder of pertial regression & officers
Con a strine by solving the following
two normal equalisms.  $\sum x_1 x_2 = b_{12.3} \sum x_2^2 + b_{13.2} \sum x_1 x_2$  $\sum x_1 x_3 = b_{12.3} \sum x_2 x_1 + b_{13.2} \sum x_2^2$  $\begin{array}{c} \text{fwther } & \text{S-Pvid} \\ \text{b}_{12\cdot3} = & \left( \sum x_1 x_2 \right) \left( \sum x_3 \right)^2 - \left( \sum x_1 x_3 \right) \left( \sum x_2 x_3 \right) \\ & \left( \sum x_2^2 \right) \left( \sum x_3^2 \right) - \left( \sum x_2 x_3 \right)^2 - \left( i \right) \end{array}$ 

b 13.2 = [(\(\(\tau\_1\x\_3\)(\(\tau\_2\))] - [(\(\tau\_1\x\_2\)(\(\tau\_3\x\_2\))] +9f X20nX, lX3  $(x_2 - x_2) = 5_{21.3}(x_1 - x_1) + 5_{23.}(x_3 - x_3)$  $x_{2} = \frac{5}{21.3}x_{1} + \frac{5}{23.1}x_{3}$ when 521.3 \$ 5 = portion regression Cephint  $b_{21,3} = (\Sigma_{22})(\Sigma_{23}) - (\Sigma_{22})(\Sigma_{23})(\Sigma_{23})$  $(52^{2})(52^{2})-(52,2)^{2}$ 

 $523.1 = (\Sigma_{2}^{2} \chi_{3})(\Sigma_{1}^{2}) - (\Sigma_{2}^{2} \chi_{1})(\Sigma_{3}^{2} \chi_{1})$   $(\Sigma_{3}^{2})(\Sigma_{1}^{2}) - (\Sigma_{3}^{2} \chi_{1})^{2}$ 

# 9 f @. X3 on X, 8 X2  $(x_3 - \overline{x}_3) = b_{31\cdot 2}(x_1 - \overline{x}_1) + b_{32\cdot 1}(x_2 - \overline{x}_2)$ => x3 = 531.2 x, + 5 32.1 x2 vehere 531.2 & 532.1 cre persone Co-copen b31,2=(\(\bar{\chi}\chi\_3\chi\_1)(\bar{\chi}\chi\_2)-(\bar{\chi}\chi\_3\chi\_2)(\bar{\chi}\chi,\chi\_2)  $(\Sigma_{1}^{2})(\Sigma_{2}^{2})-(\Sigma_{1}^{2},\tau_{2})^{2}$ b 32.1= (\(\S\alpha\_3\alpha\_2\)(\(\S\alpha\_1\alpha\_1\)-(\(\S\alpha\_3\alpha\_1\)(\(\S\alpha\_3\alpha\_1\)  $(\Sigma_{2}^{2})(\Sigma_{2}^{2})-(\Sigma_{2}_{2})^{2}$ et fin) the least spore regreteres of X30 n X, 8 X2. reling Actual mean method. Afso ensimple X3, when T, = 10 8 X2 = 6. X/13 5 6 8 12 141 X2 16 10 7 4 3 2 ×3 90 72 54 42 30 12

1 × 1	2.1	12.1	X <sub>2</sub>	122	1 2	-	1~	, 2			
1	(x,-x)	1	1,5	2	22	/3	23	29	$ \chi,\chi_2 $	1 x, x3	1223
3	-5	25	16	9	81	90	40	1600	-45	-200	21
5	-3	9	10	3	9	72	22	484	-9	-66	
6	-2	4	7	0	0	54		16		-8	
8	0	0	4	-3	9	42				0	
12	4	16	3	-4	16	30	- 20	400	-16	780	24
114	6	36	2	-5	25-	12	-38	1441	-30	228	100
1										A CALL DE LA CALLESTINA	
Z7 = 48	221-	Σx,2=	42	0	2×2 =	390	223=	223=	-100	22,23=	Σx23=
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$											
/1 - 2/1 = 196 - 8 / 12 = 196 - 8 / 19 = 50											
	'')										

$$\begin{array}{lll}
x_{3} - \overline{x}_{3} &= b_{31 \cdot 2} (x_{1} - \overline{x}_{1}) + b_{32 \cdot 1} (x_{2} - \overline{x}_{2}) \\
\Rightarrow (x_{3} - 50) &= -3 \cdot 65 (x_{1} - 8) + 2 \cdot 52 (x_{2} - 7) \\
\Rightarrow x_{3} &= -3 \cdot 65 x_{1} + 2 \cdot 54 x_{2} + 61 \cdot 4 \\
&= 40 \\
&= 40 \\
\end{array}$$

169 9  $X_1 = \sum x_1/n_1 = \frac{54}{6} = 9 | X_2 = \sum x_2/n_2 = \frac{48}{6} = 8 | X_3 = \frac{5}{3} = \sum x_3/n_3 = \frac{102}{6} = 17$ 

 $\begin{array}{lll}
2f \times_{1} & \text{on} \times_{2}^{8} \times_{3} & (\times_{2}^{-2} = 20, \times_{3}^{-1} = 11) & \text{what is } \times_{1}^{7} \\
\Rightarrow & (\times_{1}^{-7} - \times_{1}^{7}) = b_{12 \cdot 3} & (\times_{2}^{-7} - \times_{2}^{7}) + b_{13 \cdot 2} & (\times_{3}^{-7} - \times_{3}^{7}) - (i) \\
\Rightarrow & \times_{1}^{-1} = b_{12 \cdot 3} & \times_{2}^{7} + b_{13 \cdot 2} & \times_{3}^{7} & - - - \\
\end{array}$ 

$$\begin{array}{l} \Rightarrow b_{12\cdot3} = (\Sigma x_1 x_2)(\Sigma x_3^2) - (\Sigma x_1 x_3)(\Sigma x_2 x_3) \\ & (\Sigma x_2^2)(\Sigma x_3^2) - (\Sigma x_2 x_3)^2 \\ = (-93 \times 454) - (-198 \times 218) \\ & (110 \times 454) - (218 \times 218) \\ = (-4222) + (43164))/(49940 - 47524) \\ = 942/2416 = 0.39// \\ \Rightarrow b_{13\cdot2} = (\Sigma x_1 x_3)(\Sigma x_2^2) - (\Sigma x_1 x_2)(\Sigma x_3 x_2) \\ & (\Sigma x_3^2)(\Sigma x_2^2) - (\Sigma x_3 x_2)^2 \\ = (-198) \times 110] - ((-93) \times (218)) \\ & (454 \times 110) - (218 \times 218) \\ = (-21780) + 20274 = -1506 \\ & (49740 - 47524) = -1506 \\ & (49740 - 47524) = -1506 \\ \hline \end{array}$$

$$\begin{array}{l} x_{2} = 20, \ x_{3} = 11, \ x_{1} = \frac{?}{2} \\ x_{1} - \overline{x}_{1} = b_{12 \cdot 3} (x_{2} - \overline{x}_{2}) + b_{13 \cdot 2} (x_{3} - \overline{x}_{3}) \\ \Rightarrow x_{1} - 9 = 0.39 (20 - 8) + (-0.62) (11 - 17) \\ x_{1} = 4.68 + 3.72 + 9 = 17.47 \end{array}$$